

# $\tau$ -polarization in the SUSY decay chain

$$\tilde{\chi}_2^0 \rightarrow \tilde{\tau}_1 \tau \rightarrow \tilde{\chi}_1^0 \tau \tau$$

Till Nattermann

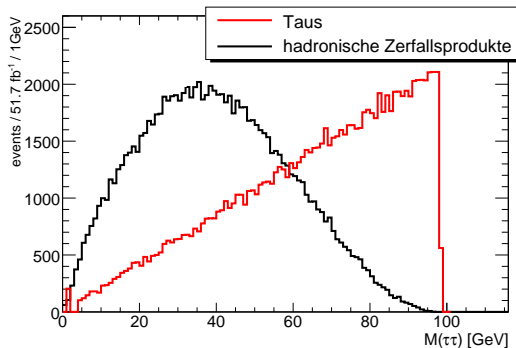
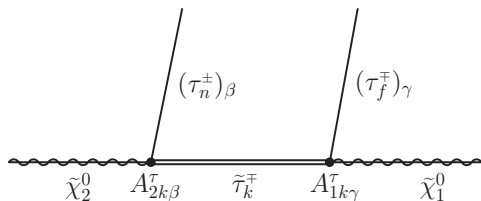
Physikalisches Institut  
Universität Bonn

Tau Mini-Workshop – Heidelberg  
14. + 15. April 2008

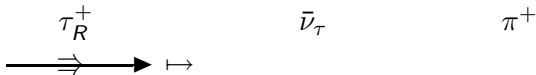


$m_{\tau\tau}$ -distribution

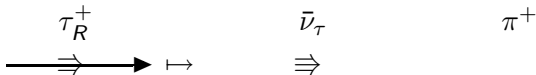
- $m_{\tau\tau}^2 = [p(\tau_n) + p(\tau_f)]^2$
- endpoint  $\leftrightarrow (m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_1^0}, m_{\tilde{\tau}})$
- shape  $\leftrightarrow \beta, \gamma$  (Pol.)

 $\tau$ s important:

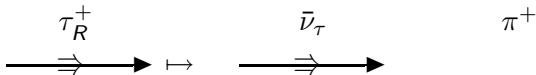
- decays in  $\tau$  favoured:
  - $m_{\tilde{\tau}_1} < m_{\tilde{\ell}}$  (mixing)
  - SU3:  $\approx \times 10$
- pol. sensitivity ( $\beta, \gamma$ )
- $\tilde{\tau}$  properties ( $m_{\tilde{\tau}}, \vartheta_{\tilde{\tau}}$ ):
  - $m_{\tilde{\tau}} \rightarrow m_{\tau\tau}^{\max}$
  - $\vartheta_{\tilde{\tau}} \rightarrow \beta, \gamma$  (Pol.)



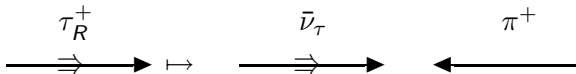
- angular momentum conservation
- handedness of neutrino
- momentum conservation



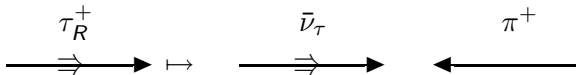
- angular momentum conservation
- handedness of neutrino
- momentum conservation



- angular momentum conservation
- handedness of neutrino
- momentum conservation



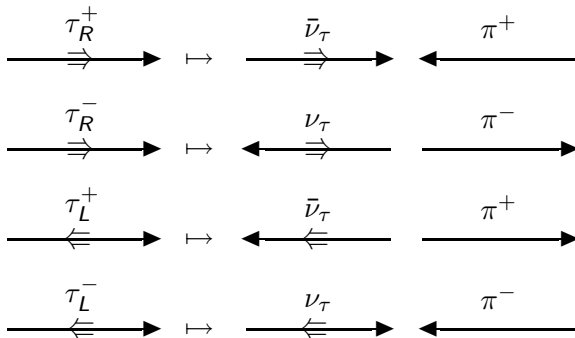
- angular momentum conservation
- handedness of neutrino
- momentum conservation



- angular momentum conservation
- handedness of neutrino
- momentum conservation

### result

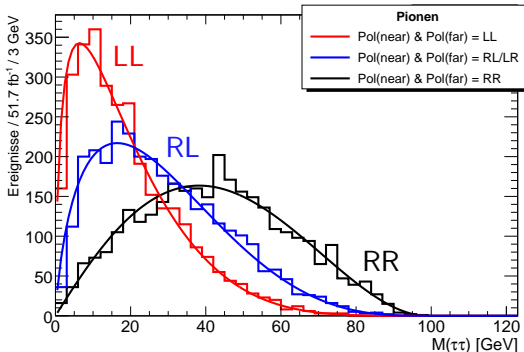
$\pi$  momentum direction in  $\tau$ -restframe specified by  $\tau$  charge and helicity (chirality)



$\tau$  rest system  $\rightarrow$  lab system

- spin-quantization-axis  $[\vec{p}(\tau)]_{\text{LAB}}$ -direction
- LORENTZ-boost  $\tau$ -rest system  $\rightarrow$  lab-system
- high and low energy  $\pi$ s



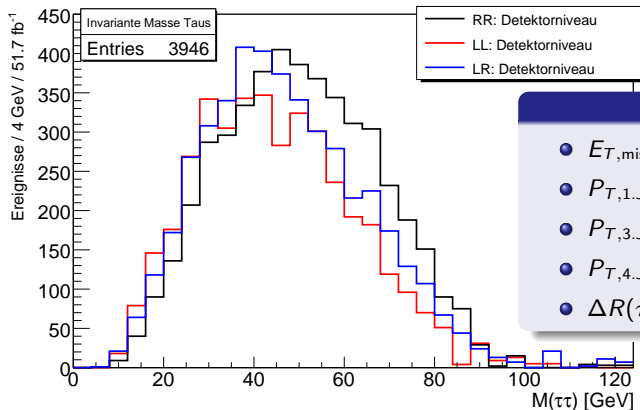

 $\tau \rightarrow \pi \nu_\tau$ 

- $m_{\pi\pi}^2 = [p(\pi_n) + p(\pi_f)]^2$
- $m_{\pi\pi}$  sensitive to polarization
- allows distinction between  $RL = LR, LL, RR$  (chirality)
- but not  $\tau_n$  and  $\tau_f$  [ $P(\tau_n) + P(\tau_f)$ ]

result:

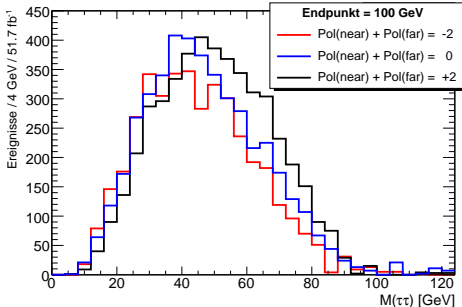
comparison theory<sup>a</sup>  $\leftrightarrow$  measurement  $\Rightarrow$  polarization

<sup>a</sup>S.Y. Choi, K. Hagiwara, Y.G. Kim, K. Mawatari, P.M. Zerwas,  
 $\tau$  Polarization in SUSY Cascade Decays, hep-ph/0612237

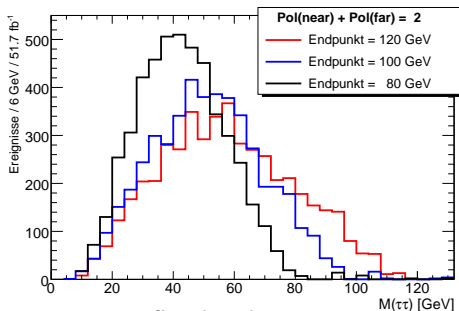


## detector level

- fakes and combinatorial background: OS-SS suppressed
- poor  $\tau$ -reconstruction for small  $M(\tau\tau)$
- endpoint (SUSY-masses)  $\leftrightarrow$  shape (polarization)



fixed endpoint  
different polarizations

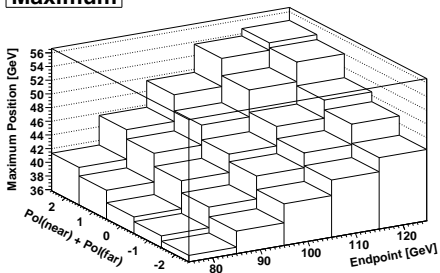


fixed polarization  
different endpoints

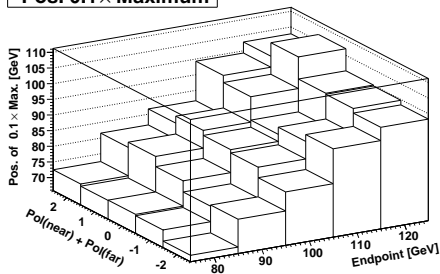
## strategy

- SUSY-masses and polarization show up differently in spectra
- fit spectra:  $f(x) = \frac{p_0}{p_1 \sqrt{2\pi}} \exp\left(-\frac{1}{2} \left(\frac{x-p_2}{p_1}\right)^2\right)$
- compare calibration  $\leftrightarrow$  measurement

Maximum



Pos of maximum  
of spectra

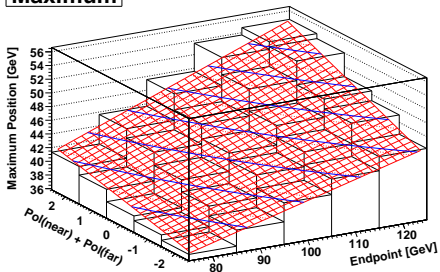
Pos.  $0.1 \times$  Maximum

Pos with  
 $f(x) = \frac{1}{10} f_{\max}$

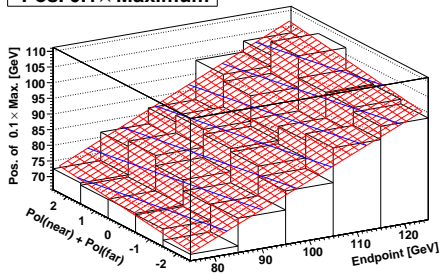
### Fit of calibration spectra

- grid of 5  $P(\tau_n) + P(\tau_f)$  and 5 endpoints  $\hat{=} 51.7fb^{-1}$
- Obs.: maximum and position with  $\frac{1}{10}$  of maximum
- calibration  $\rightarrow$  maps of observables

Maximum



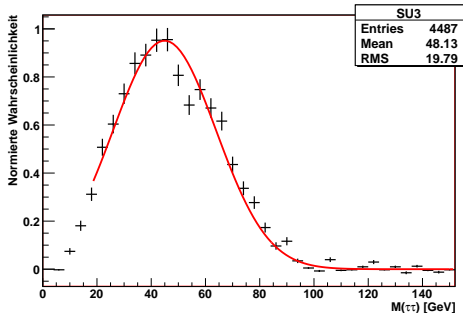
Pos of maximum  
of spectra

Pos.  $0.1 \times$  Maximum

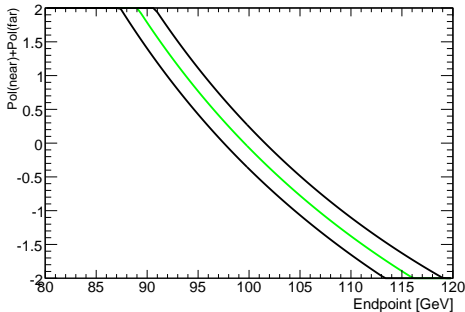
Pos with  
 $f(x) = \frac{1}{10} f_{\max}$

### Fit of observables

- $g(P(n) + P(f) = y, EP = x) = p_0 y + p_1 x + p_2 xy + p_3$
- measured observable  $\rightarrow$  equipotential line
- intersection  $\rightarrow$  polarization and endpoint

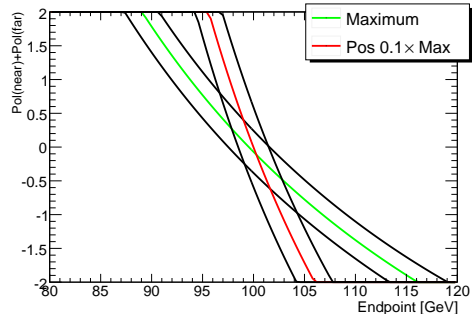


fit (SU3 spectrum)

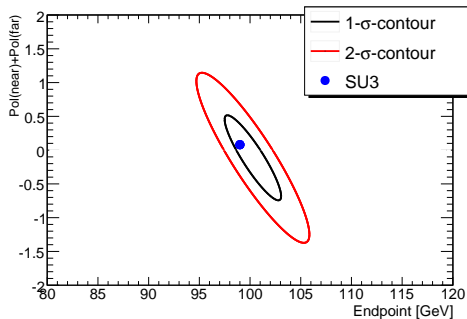
maximum with 1- $\sigma$ -lines

### measurement of observables of unknown spectrum (SU3)

- observables:  $\sigma_{\text{stat.}}$  from fit,  $\sigma_{\text{sys.}}$  with 3 binnings  $\times$  5 fit-ranges
- $\sigma^2 = \sigma_{\text{stat.}}^2 + \sigma_{\text{sys.}}^2$ .
- $\sigma_y^2 = \left(\frac{\partial y}{\partial O} \sigma\right)^2 + \sum_{i,j=1}^4 \text{cov}(p_i, p_j) \frac{\partial y}{\partial p_i} \frac{\partial y}{\partial p_j}$



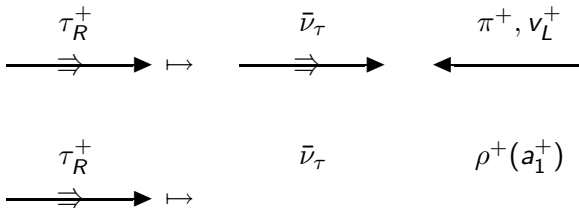
Maximum and  
 $\frac{1}{10} \times \text{Max}$



error contours and  
theoretical SU3 values

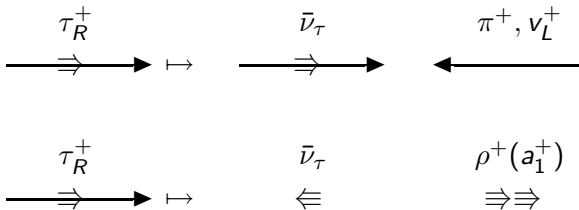
## result of measurement of SU3

- $M_{\tau\tau}^{\text{max}} = 100 \pm 3 \text{ GeV}$  (99 GeV),  $P(\tau_n) + P(\tau_f) = -0.11 \pm 0.63$  (0.08)
- 1- $\sigma$ -contour:  $\left(\frac{x}{\sigma_x}\right)^2 + \left(\frac{y}{\sigma_y}\right)^2 - 2\rho\frac{xy}{\sigma_x\sigma_y} = 1 - \rho$  with  $\rho = -0.9$
- strong experimental correlation

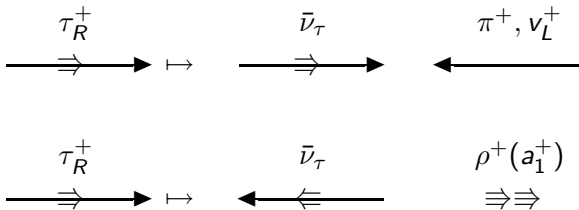


- angular momentum conservation
- handedness of neutrino
- momentum conservation

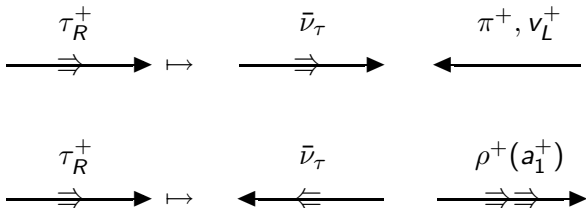




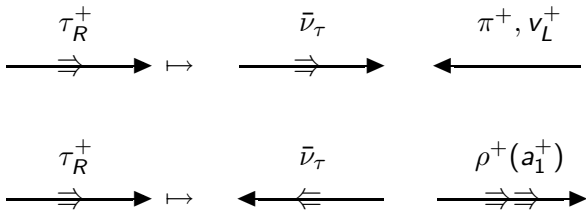
- angular momentum conservation
- handedness of neutrino
- momentum conservation



- angular momentum conservation
- handedness of neutrino
- momentum conservation



- angular momentum conservation
- handedness of neutrino
- momentum conservation

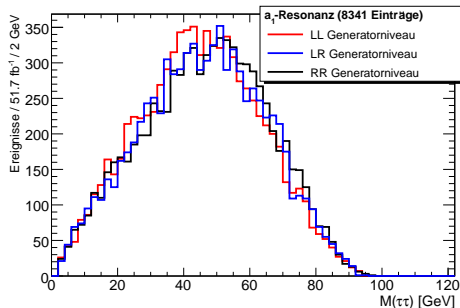


- angular momentum conservation
- neutrino handedness
- momentum conservation

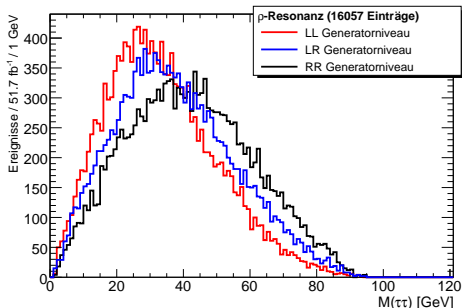
result:

longitudinal (transversal)  $\rho, a_1$ : same (opposite) momentum direction as  $\pi$

$$\frac{1}{\Gamma_\nu} \frac{d\Gamma_\nu}{d \cos \vartheta} = \underbrace{\left( \frac{m_\nu^2}{m_\tau^2 + 2m_\nu^2} (1 - P_\tau \cos \vartheta) \right)}_{\text{transversal}} + \underbrace{\left( \frac{\frac{1}{2} m_\tau^2}{m_\tau^2 + 2m_\nu^2} (1 + P_\tau \cos \vartheta) \right)}_{\text{longitudinal}}$$



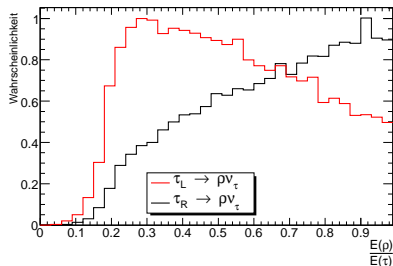
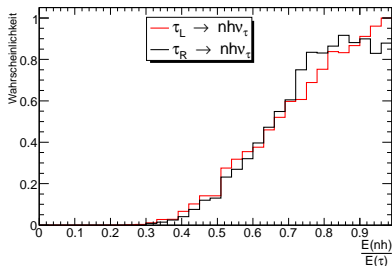
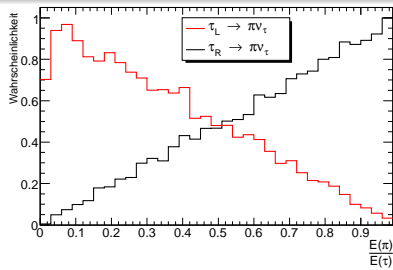
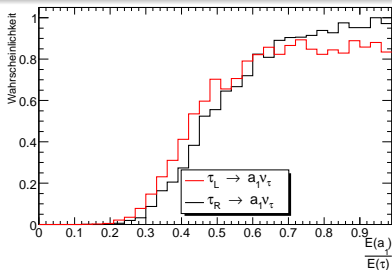
$[a_1 a_1]_{RR} \approx [a_1 a_1]_{LL}$   
independent of polarization



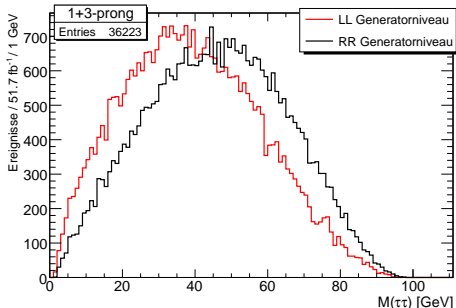
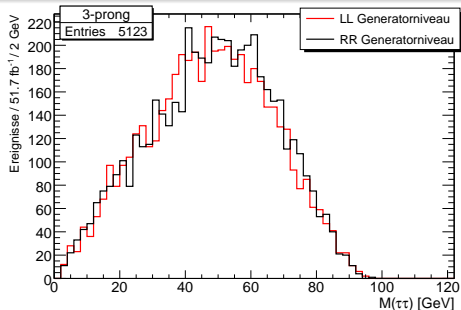
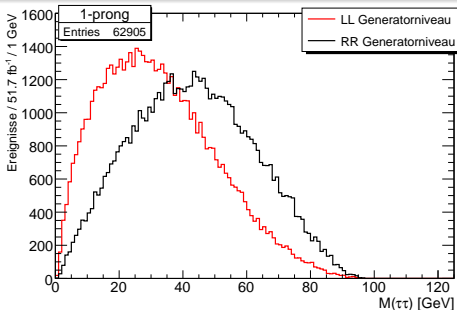
$[\rho\rho]_{RR} > [\rho\rho]_{LL}$   
dependent on polarization

## vector mesons

- $a_1$  pol. independent,  $\rho$  depends on pol.
- selection  $\tau$ -decays  $\rightarrow$  spectra with max (min) dependence on pol.
- compare  $[\pi\pi]$  and  $[a_1 a_1]$ -spectra



- fragmentation functions (arbitrary units)  $\left( \frac{E(\text{visible})}{E(\tau)} \right)$  generator level
- decay via  $\rho$  and  $\pi$  is polarization dependent, rest not



## prong selection

**1-prong:**  $\rho$ ,  $\pi$ ,  $K$ ,  $a_1$

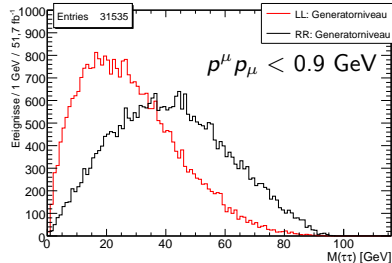
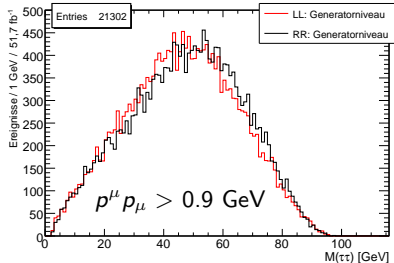
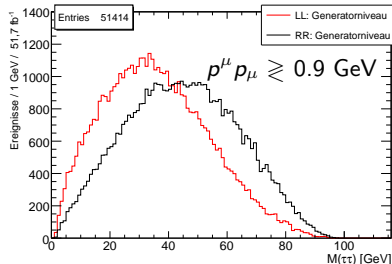
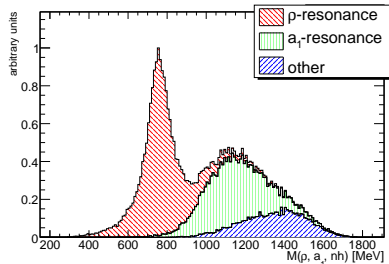
mostly dependent on polarization

**3-prong:**  $a_1$ , other decays

independent of polarization

**but:** 3-prong poor statistics (5%)

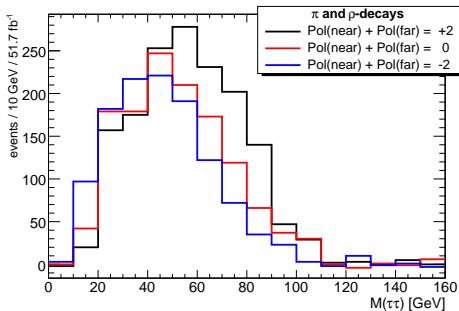
→ poor endpoint determination



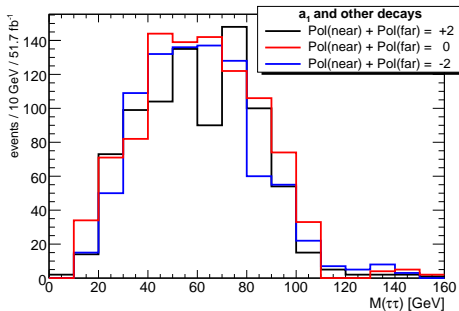
- resonant structure allows decay ID
- more efficient than prong sel.

- reconstruction inv. mass needed
- reality: resonances get broader





$\rho$  and  $\pi$  and  $K$  decays  
dependent on polarization



$a_1$  and other decays  
independent of polarization

### selection of decay modes (from MC truth) on detector level

- $a_1$  pol. independent,  $\rho$  depends on pol.
- 4000 (all dec.) = 800 ( $a_1$ &other) + 1500 ( $\rho$ ,  $\pi$ ,  $K$ ) + 1700 (mixed)
- gain in information compensated by loss of statistics

improve sensitivity with selection of  $\tau$  decay modes:

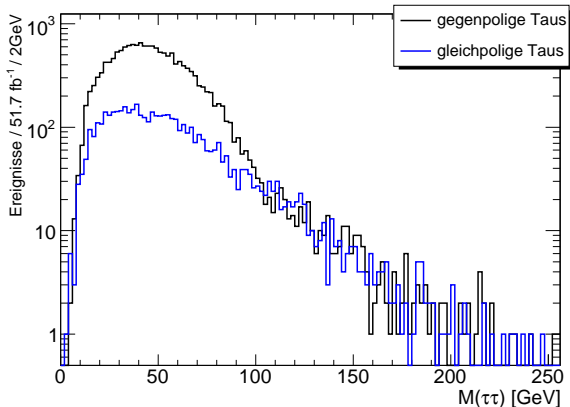
- 1 compare polarization affected and non-affected spectra
- 2 but: requires discrimination of decay modes
- 3 maybe: gain of information is overcompensated by loss of statistics

results with shape related observables for  $51.7fb^{-1}$ :

- 1 endpoint =  $100 \pm 3$  GeV (theoretical: 99GeV)
- 2 sum of polarization =  $-0.11 \pm 0.63$  (theoretical: +0.08)
- 3 strong experimental correlation

backup

# fakes and combinatorial background



## OS - SS

- $M(\tau\tau) > M(\tau\tau)_{\max} \Rightarrow$  fakes and combinatorial background
- $M(\tau\tau) > M(\tau\tau)_{\max} : [\tau^{\pm}\tau^{\pm}] \approx [\tau^{\pm}\tau^{\mp}]$  (uncorrelated)
- $\tilde{\chi}_4^0 \rightarrow \tilde{\chi}_1^{\pm}\tau^{\mp}\nu_{\tau} \rightarrow \tilde{\tau}^{\pm}\nu_{\tau}\tau^{\mp}\nu_{\tau} \rightarrow \tau^{\pm}\tilde{\chi}_1^0\nu_{\tau}\tau^{\mp}\nu_{\tau}$